



### Structural model

DESCRIPTION:  
[LONGITUDINAL]

DESCRIPTION: Optional text describing the model

[LONGITUDINAL] section

Contains the structural model with:

- **input = { }** list  
parameters that are estimated or used as regressor variables.
- **PK: block**  
permits to define PK models using macros, and to link the administration information of the data set with the model.
- **EQUATION: block**  
mathematical equations including ODEs and DDEs.
- **DEFINITION: block**  
used to define a random variable and its probability distribution.
- **OUTPUT: block**  
contains the [LONGITUDINAL] section outputs.
  - **output = { }** list  
identifies the predictions or the modeled outputs that are fitted against the data set observations.
  - **table = { }** list  
parameters or variables outputted in the result folder of Monolix.

input = { }

PK:

EQUATION:

DEFINITION:

OUTPUT:

output = { }  
table = { }

### Modeling discrete data with DEFINITION:

#### Time-to-event model

DEFINITION:

Event = {type=event, maxEventNumber=1, hazard=h}

- **Event:** name of the random variable, can be replaced by any name. It should be listed in the outputs, to be matched to the observed data.
- **hazard:** hazard function, can be defined via an expression in EQUATION:.
- Indicating the maximum number of events in the **maxEventNumber** argument speeds up calculations.

#### Count model

DEFINITION:

CountNumber = {type=count, P(CountNumber=k) = ...}

- **CountNumber:** name of the random variable, can be replaced by any name. It should be listed in the outputs, to be matched to the observed data.
- **k** is a mandatory name for the values. The probability mass function **P(CountNumber=k)** should be defined as a function of **k** and individual parameters.
- It is possible to define directly the log of the probability mass function with:  $\log(P(\text{CountNumber}=k)) = \dots$

#### Categorical model

DEFINITION:

level = {type = categorical,  
categories = {0, 1, 2},  
 $\logit(P(\text{level} \leq 0)) = \text{th1}$   
 $\logit(P(\text{level} \leq 1)) = \text{th1} + \text{th2}$ }

- **categories:** list of ordered categories, as increasing successive integers.
- **P(Y=i):** probability of a given category integer i, for the observation named Y. A transformed probability can be provided instead of a direct one. The transformation can be log, logit, or probit.
- The model is completely defined by the probability mass functions  $P(Y=i)$  for each category, or the cumulative probabilities  $P(Y \leq i)$ .
- When the value of a probability can be deduced from others, its definition can be spared.

### PK: macros

#### Arguments

##### Compartment characteristics

amount	Variable for drug amount in the compartment
concentration	Variable for drug concentration in the compartment
volume, V	Compartment volume

##### Administration

adm	Administration type to map with ADMINISTRATION ID from dataset, optional: default value is 1
-----	--

##### Targets

cmt	Label of compartment (integer)
target	ODE variable

##### Absorption

Tk0	Zero-order duration
ka	First-order rate
p	Fraction of absorbed drug

##### Delays

Tlag	Lag time
Ktr	Transit rate
Mtt	Mean transit time

##### Transfers

kt	Transfer rate from one compartment to another
kij, kji	Transfer rates between compartments i and j
ke0	Transfer rate to an effect compartment

##### Elimination

k	Elimination rate
Cl	Clearance
Vm, Km	Michaelis-Menten elimination

#### pkmodel macro

**pkmodel**(V, k/Cl/(Vm, Km),  
Tlag/(Ktr, Mtt), p, Tk0/ka,  
(k12, k21), (k13, k31), ke0)

Defines common PK models with a list of parameters. Single administration type and single elimination only.

#### Administration macros

Administration macros apply the doses from the dataset to the model. Dose types indicated in the column ADMINISTRATION ID are mapped with the argument adm.

#### Targeting a compartment

**absorption**(adm = ..., cmt = ...,  
Tlag/(Ktr, Mtt), p, Tk0/ka)

For first-order or zero-order absorption arriving in cmt compartment.

**iv**(adm = ..., cmt = ..., Tlag, p)

For bolus or infusion into cmt.

#### Targeting an ODE variable

**depot**(adm = ..., target = ...,  
Tlag/(Ktr, Mtt), p, Tk0/ka)

For first-order or zero-order absorption, bolus or infusion. Amount applied to the ODE variable in target.

**reset**(adm = ..., target = ...)

Resets the target variable to its initial value at the corresponding dosing times in the dataset (dose value not used).

**empty**(adm = ..., target = ...)

Sets the target variable to 0 at the corresponding dosing times in the dataset (dose value not used).

#### Compartment macros

**compartment**(cmt = ...,  
amount/concentration = ...,  
volume = ...)

Defines a compartment that can be used in other macros. Needs to be defined first.

**peripheral**(kij, kji,  
amount/concentration = ...,  
volume = ...)

Defines a peripheral compartment of label j with two transfers of drug amount from and toward the compartment of label i.

**effect**(cmt = ..., ke0,  
concentration = ...)

Defines an effect compartment with a transfer of drug from compartment cmt.

**transfer**(from = i, to = j, kt)

Unidirectional transfer process from compartment i to compartment j.

#### Elimination macro

**elimination**(cmt = ...,  
k/Cl/(Vm, Km))

Defines an elimination from compartment cmt.

Legend:

/: Mutually exclusive  
(): Mutually dependent  
Mandatory arguments

### Syntax for equations and ODEs

#### Syntax

**ddt\_x:** time derivative of variable x (x can be any name)

**t\_0:** initial value of time

**x\_0:** initial value of variable x

**if, elseif, else, end:** conditional statements

**a\*b, a/b, a^b:** math operators

**a==b, a<b, a<b, a>=b, a&b, a|b:** logical operators

**exp, log, log10, sqrt, cos, sin, factln, max, min ...:** math functions

#### Keywords

**t:** time

**tDose:** time of the last administered dose

**amtDose:** amount of the last administered dose

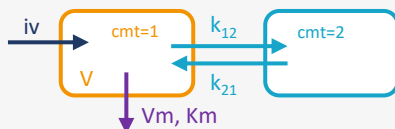
**infDose:** infusion time of the last administered dose

**delay(x,tau):** delay function for DDEs

**odeType = stiff:** use a stiff ODE solver (add in EQUATION:)

Comments begin with ;

### Two-compartment model with iv bolus/infusion and Michaelis-Menten elimination



This model is available in the PK models library.

```
[LONGITUDINAL]
input = {V, Vm, Km, k12, k21}

EQUATION:
Cc = pkmodel(V, Vm, Km, k12, k21)

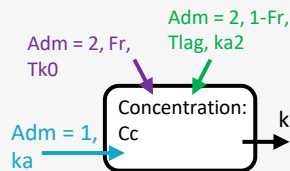
OUTPUT:
output = Cc
```

### Two formulations: 1<sup>st</sup> order absorption and mixed 0-order/ 1<sup>st</sup> order absorption

```
[LONGITUDINAL]
input = {V, ka, Tk0, ka2, Fr, k}
```

```
PK:
compartment(cmt = 1, volume = V, concentration = Cc)
absorption(adm = 1, cmt = 1, ka)
absorption(adm = 2, cmt = 1, Tk0, p = Fr)
absorption(adm = 2, cmt = 1, Tlag = Tk0, ka = ka2,
           p = 1-Fr)
elimination(cmt = 1, k)
```

```
OUTPUT:
output = Cc
```



The two formulations should be distinguished in the dataset with the column ADMINISTRATION ID.

### PK-urine: joint model with plasma concentration and amount in urine

```
[LONGITUDINAL]
input = {ka, Cl, V, p_urine}
```

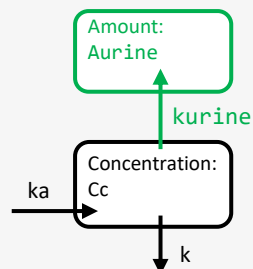
```
PK:
depot(adm = 1, target = Ac, ka)
empty(adm = 2, target = Aurine)
```

EQUATION:

```
k_urine = p_urine*Cl/V
k_non_urine = (1-p_urine)*Cl/V
```

```
t_0 = 0
Ac_0 = 0
Aurine_0 = 0
ddt_Ac = - k_non_urine*Ac - k_urine*Ac
ddt_Aurine = k_urine*Ac
Cc = Ac/V
thalf = log(2)*V/Cl
```

```
OUTPUT:
output = {Cc, Aurine}
table = {thalf}
```



Times of emptying of urine compartment are encoded in the dataset as pseudo-doses with ADMINISTRATION ID = 2. A table of values for the elimination half-life thalf is outputted in the result folder at each observation time.

### Auto-induction model for time-varying clearance

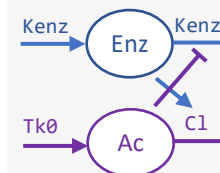
```
[LONGITUDINAL]
input={Tk0, V, Cl, Kenz, IC50}
```

```
PK:
depot(target=Ac, Tk0)
```

```
EQUATION:
t_0 = 0
Ac_0 = 0
Enz_0 = 1
```

```
ddt_Ac = - Cl/V*Ac*Enz
ddt_Enz = Kenz - Kenz * (1 - Cc/(Cc+IC50)) * Enz
Cc = Ac/V
```

```
OUTPUT:
output = {Cc}
```



The drug stimulates its own metabolism via induction of the metabolic enzyme expression.

### PK – PD – TTE: joint model for plasma concentration, tumor volume and death

```
[LONGITUDINAL]
input = {V, Cl, Q, V2, Vm, Km, Mini, kp, kd,
        R, lambda0, betaM}
```

```
;plasma concentration model
PK:
compartment(cmt = 1, amount = Ac, volume = V,
            concentration = Cc)
peripheral(k12 = Q/V, k21 = Q/V2)
elimination(cmt = 1, Cl)
elimination(cmt = 1, Vm, Km)
iv(adm = 1, cmt = 1)
```

```
;tumor growth model
EQUATION:
odeType = stiff
t_0 = 0
M_0 = Mini
ddt_M = (kp - kd*Cc*exp(-R*t))*M
Msat = min(1000, M)
```

```
;time-to-event (death) model
lambda = lambda0*exp(betaM*Msat)
DEFINITION:
death = {type = event, eventType = exact,
        maxEventNumber = 1, hazard = lambda}
```

```
OUTPUT:
output = {Cc, M, death}
```

The statement **odeType = stiff** permits to use a stiff (implicit) ODE solver.

### Dose-dependent bioavailability

Using dose-related keywords: amtDose

```
[LONGITUDINAL]
input = {ka, k, V, D50}
```

```
PK:
F = amtDose / (amtDose + D50)
Cc = pkmodel(ka, V, k, p = F)
```

```
OUTPUT:
output = {Cc}
```

Using a regressor containing the dose information

```
[LONGITUDINAL]
input = {ka, k, V, DoseReg, D50}
DoseReg = {use = regressor}
```

```
PK:
F = DoseReg / (DoseReg + D50)
Cc = pkmodel(ka, V, k, p = F)
```

```
OUTPUT:
output = {Cc}
```

### Count model: zero - inflated Poisson model

```
[LONGITUDINAL]
input = {lambda0, nu, f}
```

```
EQUATION:
lambda = lambda0*exp(-t/nu)
```

```
DEFINITION:
CountNumber = {type = count,
               if k==0
                 Pk = exp(-lambda)*(1-f) + f
               else
                 Pk = exp(k*log(lambda) - lambda - factln(k))*(1-f)
               end
               P(CountNumber = k) = Pk}
```

```
OUTPUT:
output = CountNumber
```

The output is the number of events (in {0, ..., infinity}) with an inflation of zero counts. Lambda decreases exponentially over time.